

## 5.4 Notes: Double Angle Formulas

### Double Angle Identities

$$\sin 2u = 2 \sin u \cos u$$

$$\cos 2u = \cos^2 u - \sin^2 u$$

$$\tan 2u = \frac{2 \tan u}{1 - \tan^2 u}$$

$$= 1 - 2 \sin^2 u$$

$$= 2 \cos^2 u - 1$$

**NOTE:**  $\sin^2 u \neq \sin 2u$

$\cos^2 u \neq \cos 2u$

$\tan^2 u \neq \tan 2u$

**Ex: 1 Solve**

a.)  $2 \cos x + \sin 2x = 0$

b.)  $3 \sin^2 x + \cos 2x - 2 = 0$

**You Try:** Solve  $\cos 2x + \cos x = 0$

**Ex: 2** Given  $\cos \theta = \frac{5}{13}$ , and  $\frac{3\pi}{2} < \theta < 2\pi$  find  $\sin 2\theta$ ,  $\cos 2\theta$ ,  $\tan 2\theta$ .

**You Try:** Given  $\tan u = \frac{8}{15}$ , and  $\pi < u < \frac{3\pi}{2}$ , find  $\sin 2\theta$ ,  $\cos 2\theta$ ,  $\tan 2\theta$ .